Decomposition of brain diffusion imaging data uncovers latent schizophenias with distinct patterns of white matter anisotropy

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Abstract

Fractional anisotropy (FA) analysis of diffusion tensor-images (DTI) has yielded inconsistent abnormalities in schizophrenia (SZ). Inconsistencies may arise from averaging heterogeneous groups of patients. Here we investigate whether SZ is a heterogeneous group of disorders distinguished by distinct patterns of FA reductions. We developed a Generalized Factorization Method (GFM) to identify biclusters (i.e., subsets of subjects associated with a subset of particular characteristics, such as low FA in specific regions). GFM appropriately assembles a collection of unsupervised techniques with Non-negative Matrix Factorization to generate biclusters, rather than averaging across all subjects and all their characteristics. DTI tract-based spatial statistics images, which output is the locally maximal FA projected onto the group white matter skeleton, were analyzed in 47 SZ and 36 healthy subjects, identifying 8 biclusters. The mean FA of the voxels of each bicluster was significantly different from those of other SZ subjects or 36 healthy controls. The eight biclusters were organized into four more general patterns of low FA in specific regions: 1) genu of corpus callosum (GCC), 2) fornix (FX) + external capsule (EC), 3) splenium of CC (SCC) + retrolenticular limb (RLIC) + posterior limb (PLIC) of the internal capsule, and 4) anterior limb of the internal capsule. These patterns were significantly associated with particular clinical features: Pattern 1 (GCC) with bizarre behavior, pattern 2 (FX + EC) with prominent delusions, and pattern 3 (SCC + RLIC + PLIC) with negative symptoms including disorganized speech. The uncovered patterns suggest that SZ is a heterogeneous group of disorders that can be distinguished by different patterns of FA reductions associated with distinct clinical features.

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particularly when the abnormality is mild (Alba-Ferrara and de Erausquin, 2013).

To characterize the heterogeneity of structural brain abnormalities in SZ, we devised an unsupervised machine learning approach that decomposes a collection of FA images from patients with SZ into local partitions or biclusters (Cichocki, 2009; Pascual-Montano et al., 2006b; Tamayo et al., 2007). These biclusters are composed of co-differentiated white matter FA sets of voxels (i.e., voxels with low FA values) shared by subsets of subjects. Biclustering captures local and intrinsic relationships between subsets of observations (subjects) sharing subsets of descriptive features (voxels) instead of relationships between all subjects and all their descriptive features. These relationships can be weakened when all features are used in a single global model of data, as is typically done by clustering methods.

Our approach combines the advantages of a number of complementary clustering strategies into a Generalized Factorization Method (GFM, Supplementary Fig. 1) and has been previously widely applied in different biomedical problems (Harari et al., 2010; Romero-Zaliz et al., 2008b; Zwir et al., 2005b). Non-negative Matrix Factorization (NMF) algorithms have also been utilized in facial recognition (Lee and Seung, 1999), gene expression (Tamayo et al., 2007), and several other biomedical problems (Cichocki, 2009). More recently, we successfully applied a composite GFM–NMF to uncover eight different subtypes of SZ by dissecting genome wide association studies into biclusters composed of distinct sets of genetic variants and clinical symptoms of SZ patients (Arnedo et al., 2013, 2014).

In the current study, we applied the GFM–NMF methodology to examine a sample of SZ patients and healthy controls whose diffusion-weighted brain images were processed using Tract Based Spatial Statistics (TBSS) (Smith et al., 2006). We refer to the output of TBSS, which is the locally maximal FA projected onto the group white matter skeleton, as an FA-TBSS image. We searched for biclusters reflecting different FA patterns that can be shared by distinct subsets of SZ patients. Then we evaluated the significance of each bicluster by comparing the differential FA within a bicluster with that exhibited by healthy controls, as well as with that shown in other individuals with SZ who were not present in the bicluster. We then analyzed the anatomical location of DTI abnormalities identified in the biclusters. In the final step, we cross-correlated the uncovered biclusters with collected descriptions of clinical features of the patients including positive and negative symptoms scores as defined by the Scale for the Assessment of Positive Symptoms (SAPS) and the Scale for the Assessment of Negative Symptoms (SANS) (Andreasen, 1984).

The method illustrated here is able to agnostically decompose FA-TBSS images and to distinguish subsets of SZ patients using white matter FA patterns, just as we decomposed SZ into subtypes with complex relations between sets of genotypes and sets of clinical phenotypes (Arnedo et al., 2014). These abnormalities may suggest distinct etiologies in patients diagnosed with SZ, characterized by different brain areas leading to distinct symptoms and clinical outcomes. The software is available upon request from the authors.
Methods

Study sample

The participants included in the study were drawn from a population of volunteers for studies of brain structure and function at the Conte Center for the Neuroscience of Mental Disorders at Washington University Medical School, St. Louis. All participants gave written informed consent for participation following a complete description of the risks and benefits of the study. Participants consisted of 47 individuals (mean age = 37.2 yrs; SD = 8.5) who met DSM-IV (American Psychiatric Association, 1994) criteria for SZ, and outpatients at the time of study. Diagnosis was ascertained by consensus between a research psychiatrist, who conducted a semi-structured interview, and a trained research assistant who used the Structured Clinical Interview for DSM-IV Axis I Disorders Q6 (First et al., 2002). Participants were excluded if they: (1) met DSM-IV criteria for substance abuse or dependence within the past 6 months; (2) had a clinically unstable or severe medical condition, or a medical condition that would confound the assessment of psychiatric diagnosis (e.g., hypothyroidism); (3) had a history of head injury with neurological sequelae or loss of consciousness; or (4) met DSM-IV criteria for mental retardation (mild or greater in severity). Participants include 16 females and 31 males. Ethnically, they included 1 Asian, 26 Blacks/African Americans, 19 Caucasians, and 1 multiracial. Five participants were left handed, and the rest were right handed.

Control participants consisted of 36 individuals (mean age = 36.9 yrs; SD = 9.1) who did not meet criteria for DSM-IV schizophrenia, bipolar disorder, or major depression. Other exclusion criteria were the same as for the SZ subjects. Control participants included 19 females and 17 males. Ethnically, they included 24 Blacks/African Americans and 12 Caucasians. Two control participants were left handed, and 34 were right handed.

Clinical measures

The presence and severity of positive (psychotic) symptoms was assessed using the Scale for the Assessment of Positive Symptoms (SAPS) (Andreasen, 1984). Negative symptoms were assessed using the Scale for the Assessment of Negative Symptoms (SANS) (Andreasen, 1984).

Image acquisition and pre-processing

Magnetic resonance (MR) scans were obtained using a 3 T Siemens Tim Trio scanner with a 12-channel head coil. Structural images were acquired using a sagittal magnetization-prepared radiofrequency rapid gradient-echo 3D T1-weighted sequence (TR = 2400 ms, TE = 3.16 ms, flip angle = 8°, voxel size = 1 mm isotropic). Two DTI scans (each ~ 5 min) were acquired in an oblique–axial plane with a single shot echo–planar imaging (EPI) sequence with TR = 8000 ms, TE = 86 ms, FOV 224 × 224 mm², 2 mm isotropic voxels (112 matrix with 64 slices of 2 mm), phase encoding in the A–P direction, 6/8 partial Fourier, and a parallel acceleration factor in the phase direction of 2 (GRAPPA = 2). Each DTI scan consisted of 30 volumes acquired with non-collinear diffusion-sensitizing directions at a b-value of 800 s/mm² and five interspersed volumes acquired without diffusion weighting (b-value = 0 s/mm²).

Data from the two DTI scans was concatenated and then pre-processed using FMRIB Software Library (FSL) version 4.1 (Nacsa et al., 2004). Briefly, within a given subject, a reference b = 0 volum was brain-extracted (Smith, 2002) and the diffusion-weighted volumes were registered to this reference to correct for movement and eddy current distortion (using FSL’s eddy_correct). A diffusion tensor was derived at each voxel using a standard least-squares process (FSL’s ‘dtifit’) to provide voxel-wise calculations of fractional anisotropy (FA). As a quality control mechanism, the residual error between the calculated tensor model fit and original data was computed for each slice and volume. Volumes containing slices with poor model fits were removed from the data, and the tensor was recomputed without the problematic volumes. This is an effective mechanism to identify and remove volumes with artifacts due to motion or other scanner anomalies (e.g., signal loss due to the table vibration artifact discussed in Gallichan et al., 2010).

DTI data analysis: Tract Based Spatial Statistics (TBSS)

TBSS was carried out using FSL 4.1 (Smith et al., 2006). All participants’ FA data were projected onto a mean FA image using the non-linear registration tool FNIRT to register to the FMRIB58_FA standard brain template. The registered data was thinned to create a mean FA skeleton restricted to voxels with the highest FA at the center of the major WM tracts. Following visual assessment of the optimal threshold value, the skeleton was thresholded at the recommended level of FA = 0.2 in order to remove confounding low-FA voxels, which may be caused by partial volume effects of gray matter or cerebrospinal fluid. Each participant’s aligned FA data were projected onto the skeleton by searching the maximum FA value in a region perpendicular to the skeleton (FA-TBSS image). This projection was performed for every subject.

Rationale of the Generalized Factorization Method (GFM) and the Non-negative Matrix Factorization method (NMF)

Our GFM was designed and successfully applied to identify structural or patterns or clusters (substructures) that characterize complex objects embedded in databases (Cordon et al., 2002; Romero-Zaliz et al., 2008a; Ruspiní and Zwiir, 2002; Zwiir et al., 2005a). Unfortunately, solving these kinds of complex problems cannot be resolved by a single clustering method but only by utilizing and combining the advantages of many of them, as we implemented in GFM and summarized below (Supplementary Fig. 1, see Supplementary Methods). NMF algorithms find an approximating factorization of the data: $M = W_k \times H_k$, where both decomposition matrices have only positive entries (Arnedo et al., 2013; Lee and Seung, 1999; Pascual-Montano et al., 2006b; Tamayo et al., 2007) (see Supplementary Methods). $W_k$ is an $n \times K$ matrix that defines the sub-matrix decomposition model whose columns specify how much each of the subjects contributes to each of the $k$ sub-matrices, $H_k$ is a $k \times m$ matrix whose entries represent the FA values in the $k$ sub-matrices for each of the $m$ voxels. Biclusters composed of distinct subsets of features/attributes shared by subsets of observations are derived from each sub-matrix. We integrated the GFM and NMF (GFM–NMF) to identify biclusters that can handle sparse, fuzzy and different data granularity (Cichocki, 2009).

The GFM–NMF method: identifying biclusters in FA-TBSS images

This method distinguishes four main processes (Fig. 2) where FA-TBSS images from different subjects were appropriately encoded, and multiple biclusters were determined and evaluated based on quality measures (sensitivity, generality) to select an optimal descriptive set. During selection, niches are defined to run selection locally and provide diverse but still optimal biclusters. Finally, biclusters were topologically organized and decoded into NIFTI 3D images.

Codification of the image database

Flattening each subject’s FA-TBSS image produced a vector (e.g. [voxels x subject], Fig. 2) (Cichocki, 2009). These vectors were included as rows in matrix $M$ using oro.nifti package, R version 2.15.1, where each row corresponded to a subject and each column to a tagged voxel (e.g., voxel_ID). Here, 126,586 voxels were present in the TBSS skeleton, and those cells corresponding to voxels outside the TBSS skeleton were...

Please cite this article as: Arnedo, J., et al., Decomposition of brain diffusion imaging data uncovers latent schizophrenias with distinct patterns of white matter anisotropy, NeuroImage (2015), http://dx.doi.org/10.1016/j.neuroimage.2015.06.083
removed from the matrix. The tagging order was used for posterior reconstruction of the images (see step 4). (Note that the coordinates (x, y, z) of the voxels in the $R^X \times Y \times Z$ space are not necessary for the comparison of their FA values and for reconstructing images from matrices in this particular problem.) For convenience, we utilized transposed ($MT$) and normalize matrix $M$ by scaling each column in the $[0, 1]$ interval Eq.(1):  

$$
a_{x,y,z} = 1 - \frac{a_{x,y,z} - \text{Min}(a_{x,y,z})}{\text{Max}(a_{x,y,z}) - \text{Min}(a_{x,y,z})} : \forall a_{x,y,z} \in M. \tag{1}$$  

Here the assumption is that we were interested in identifying voxels with low values relative to the rest of the patients rather than in finding voxels with the global lowest FA values. Therefore, we reversed the ordering so that low FA values produced entries near 1. This approach facilitates the search of biclusters by NMF methods, which tend to favor groupings of high values.

分解图像数据库的分解

分解矩阵 $M$ 为子矩阵 $M_k = 1, \ldots, \kappa$ 通过 FNMF 实现的 NMF 方法与默认参数。
described in Arnedo et al. (2013), where $K$ corresponds to the maximum numbers of possible sub-matrices (i.e., clusters). For $K = 2$ to $\sqrt{n}$, where $n$ is the number of subjects in the sample, apply FNMF to $M$ recurrently and calculate the corresponding $H_k$ and $W_k$ matrices. 40 different initializations of the FNMF parameters were run before selecting the best results for a given $K$ (see Sampling in Supplementary methods), which are normally enough runs to achieve internally robust sub-matrices (Arnedo et al., 2013; Pascual-Montano et al., 2006a,b).

Identification of biclusters from FNMF factorizations. Select the most representative rows and columns in the $H_k$ and $W_k$ matrices, respectively, for each one of the $k$-factors (sub-matrices) independently. Sorting the rows in $W_k$ for each column in descending order and selecting those rows that are higher than a given threshold achieves this (see below). Analogously, repeat the process for the $H_k$ matrix to select the columns. The set of selected rows (subjects) and columns (voxels) for each factor define a bicluster $B_k$, with $k = \{1, \ldots, K\}$.

The threshold (Eq. (2)) for factor $k$ in the matrix $H_k$ is defined in the unit interval [0–1] and calculated as:

$$\text{Threshold} = \max(H_k) \times (1 - \delta)$$  \hfill (2)

with $\delta$ being the degree of fuzziness of the bicluster. Here, a default $\delta = 0.35$ was utilized, which is consistent with the typical 70–30% ± 5% partition of the holdout (2-fold crossvalidation) sampling method (Mitchell, 1997) (see sensitivity analysis of this parameter in Supplementary methods).

Elimination of redundant biclusters. Because FNMF identifies biclusters in partitions with different number of clusters $K$, it is possible that the same bicluster can be generated more than one time. Biclusters with a high degree of overlap are considered once. The degree of overlap between two biclusters was assessed by calculating the pairwise probability of intersection among them based on the hypergeometric distribution ($P_{\text{hyp}}$, Eq. (3)) (Tavazoie et al., 1999; Zwir et al., 2005a):

$$P_{\text{hyp}}(B_i, B_j) = \frac{1 - \frac{1}{n-1} \sum_{q=0}^{p-1} \left( \begin{array}{c} h \\ q \end{array} \right) \left( \begin{array}{c} n-h \\ q \end{array} \right) \left( \begin{array}{c} g \\ h \end{array} \right) \right)}{\binom{h}{0}C_{\frac{1}{2}}(\binom{n}{h})}, \quad h = |B_i|; n = |B_j|; p$$ \hfill (3)

where $p$ observations (subjects/features/voxels) belong to bicluster $B_i$ with size $h$, and also belong to a bicluster $B_j$ of size $n$; and $g$ is the total number of observations. Therefore, the lower the $P_{\text{hyp}}$, the higher the overlapping and the better the co-cluster coincidence. Here, a default $P_{\text{hyp}} < 1E-03$ was utilized (Arendo et al., 2013; Tavazoie et al., 1999; Zwir et al., 2005b). Biclusters harboring <10% of the total number of subjects were not considered to avoid a trend to obtain singleton biclusters.

Optimization and organization of the factorized image database

Evaluation of biclusters. Biclusters were characterized by two objectives: specificity and generality. Specificity is defined as the frequency of voxels displaying low FA values in a bicluster relative to the entire FA-TBSS image (Eq. (4)):

$$\text{Specificity}(B_i) = \frac{\# \text{ voxels in } B_i}{\# \text{ total voxels}}$$  \hfill (4)

where voxels in $B_i$ correspond a subset of low FA values (Eq. (1)) shared by a particular subset of subjects, and total voxels correspond to the entire voxels in an FA-TBSS image (Eq. (4)). Here the assumption is that our data are sparse, and thus, large number of voxels may produce associations with diverse brain regions (suggesting low specificity), whereas a small number of voxels tend to be concentrated in a single or a few cohesive locations (suggesting high specificity) (Arendo et al., 2014; Cordon et al., 2002; Ruspini and Zwir, 2002; Zwir et al., 2005a).

Generality is defined in the same fashion but with respect to the subjects in a bicluster (Eq. (5)):

$$\text{Generality}(B_i) = \frac{\# \text{ subjects in } B_i}{\# \text{ total subjects}}$$  \hfill (5)

where subjects in $B_i$ share particular subsets of voxels with low FA values. Here the assumption is that biclusters generated with a small maximum number of clusters $K$ (low granularity) tend to include a large number of subjects, and thus, they are likely to share a more heterogeneous set of features (voxels with low FA values) than a smaller group of subjects from a bicluster generated when using a large $K$ value (high granularity) (Arendo et al., 2014; Cordon et al., 2002; Ruspini and Zwir, 2002; Zwir et al., 2005a), see sensitivity analysis of parameters in Supplementary methods).

Another indirect objective considered for the evaluation of biclusters is the generation of diverse patterns that completely describe objects (patients). Therefore, our approach evaluates the sensitivity and generality objectives described above in a local niche (Deb, 2001a,b; Ruspini and Zwir, 2002; Zwir et al., 2005a). Both sensitivity and specificity measurements are based on counting objects within a bicluster without distinguishing among them (e.g., # subjects). However, diversity differentiates which objects are within a bicluster, and thus, biclusters harboring distinct objects are allocated in different niches. These niches are calculated using Jaccard’s metric between biclusters (Romero-Zaliz et al., 2008a,b) (i.e., inclusion of subjects, Eq. (6)):

$$\text{Niching}(B_i, B_j) = \frac{\text{Sim}(B_i, B_j)}{\text{Sim}(B_i)} > \gamma$$  \hfill (6)

where $B_i$ and $B_j$ were the two different biclusters, the 5 functional retrieved the subjects in the biclusters in a particular niche, and $\gamma$ (0.7) is size of the niche determined by the degree of overlapping/intersection between biclusters. Here the assumption is that the niches are equivalence classes dictated by the degree of overlapping/inclusion between subjects in the biclusters.

Selection of optimal biclusters using multibjective and multimodal optimization techniques. Optimal biclusters were obtained as a tradeoff between two opposing objectives: sensitivity and generality (Arendo et al., 2014; Deb, 2001a,b; Ruspini and Zwir, 2002; Zwir et al., 2005a). A Pareto-optimization strategy searches for solutions that are non-dominated in the sense that there was no other solution superior in all objectives being selected (i.e., close to Minimum Description-Length (MDL) (Rissanen, 1989)). The dominance relationship as a minimization problem is defined as (Eq. (7)):

$$a \triangleright b \iff \forall i \; O_i(a) \leq O_i(b) \; \land \; \exists i \; O_i(a) < O_i(b)$$  \hfill (7)

where the $O_i$ and $O_j$ are either specificity or generality objectives. Optimization of small sets of biclusters was exhaustively implemented, whereas evaluation of large sets is approached by genetic algorithms, as described in Harari et al. (2010) and Romero-Zaliz et al. (2008a,b).

MDL-like optimization approaches recommend the “best” model by optimizing the sum of the model accuracy and its size (single objective), and encode the information into bits. Pareto-based optimization solves the original multi-objective problem by treating the model-quality criteria of accuracy and size as two separate quality measures, and is more generic than MDL since it can cope with any kind of non-commensurable model-quality criteria (Freitas, 2004; Ruspini and Zwir, 2002; Zwir et al., 2005a).

Our approach applied the non-dominance relationship described above locally. That is, it identifies all non-dominated optimal biclusters that have no better solution (i.e., multiobjective) in a niche (i.e., multimodality) or equivalence class defined based on...
the non-dominance partial order (Deb, 2001a; Ruspini and Zwir, 2002; Zwir et al., 2005a). Then, given two biclusters where one of them has the same or even worst sensitivity and generality than the other but correspond to different sets of subjects, both biclusters will be preserved because they are in different niches. Biclusters containing < 10% of the total number of subjects were not considered to avoid a trend yielding singleton biclusters. Statistical significance was used as an independent validation measurement of the bicluster quality (see below).

**Topological organization of optimal biclusters into hierarchies.** Non-dominated biclusters in each niche were top-down organized into hierarchies (networks or sub-graphs) from the most general (i.e., the bicluster containing the greatest number of subjects, see above) to the most specific (i.e., the bicluster containing the smallest and most cohesive set of voxels, as described above). Note that one bicluster can belong to more than one niche based on the Niching function described above, or hierarchies can be disjoint when mapping to independent sets of subjects. Biclusters are renamed as $B_{i,j}$, where $i$ corresponds to a particular hierarchy, and $j$ to the order in such hierarchy (smallest $j$-value indicates the most general and top level bicluster).

**Folding the optimal biclusters into NIfTI 3D images for visualization**

A new NIfTI 3D image was generated for each bicluster from its corresponding matrix representation to visualize the location of specific FA voxels on the FA-TBSS images using the oro.nifti package in R version 2.15.1. The tagging order ($\text{voxel}_{i,j}$, see step (1)) used for encoding FA-TBSS images was utilized in a reverse fashion.

**Sensitivity analysis of parameters**

Comparisons between algorithms (i.e., the bioNMF and the FNMF biclustering methods) and evaluation of parameters, including initialization and stopping criteria, outlier detection, number of clusters, and degree of fuzziness in the NMF methods are described in Supplementary Methods.

**Sampling analysis**

Sampling analysis was performed by leave-one-out and leave-one-bicluster-out as described in Supplementary methods.

**Statistical analysis**

Statistical analysis was performed by using one-way ANOVA, pairwise t-test and Bonferroni correction (R version 2.15.1) as described in Supplementary methods.

**Statistical analysis**

Identification of biclusters was unbiased without a prior knowledge of the anatomical location of voxels and/or the clinical symptoms of the subjects. Using internal criteria in cluster evaluation is biased towards algorithms that use the same cluster model (Bezdek, 1998). Therefore, external evaluations based on criteria that were not used for clustering, such as tests based on ANOVA and its F-statistic, are often added to the cluster evaluation (Fürber et al., 2010). To assess the statistical significance of the findings, we compared the average FA in the set of voxels of each bicluster with the average FA value in the same voxels of either SZ subjects who were not included in the bicluster or healthy controls by one-way ANOVA and pairwise t-test (R version 2.15.1) and applying Bonferroni correction. Evaluation of global differences in FA between all SZ subjects who were not included in the bicluster or healthy controls (see Statistical analysis, Methods, p-value > 0.81). A partition of the images corresponding to the patients with SZ using GFM–NMF uncovered eight optimal local partitions or biclusters, where each bicluster encoded a subset of subjects characterized by a similar degree of FA reduction in a particular subset of voxels. This method allowed any given subject and/or voxel to belong to more than one bicluster or to none of them (see Methods). The mean FA of the voxels in each of the eight biclusters significantly differed from the mean FA for voxels in the same location in either the other SZ subjects not included in that bicluster or from the healthy controls after correction for multiple comparisons (see Statistical analysis, Methods, Table 1, Figs. 3–4). This suggests that the biclusters should separately explain a large part of the variability in the population. In fact, 41 of the 47 SZ subjects were included in at least one bicluster (Table 1), which accounted for >95% of the FA variance across subjects (in the population) and suggests a high degree of generality. The biclusters varied in terms of their size, based on the associated numbers of subjects and shared voxels. For example, one general bicluster (i.e., one having high coverage) contained 21 subjects and 9744 voxels, while another specific bicluster (i.e., one having low coverage) contained only 5 subjects and 1322 voxels. While generality implies a large coverage of the sample; specificity displays smaller but more cohesively arranged and shared sets of FA voxels in the sample. The latter two biclusters did not overlap, and thus were associated with FA reductions in different brain regions, as expected. On the other hand, another pair of biclusters containing 15 subjects with 5147 voxels and 5 subjects with 2637 voxels respectively, showed a high degree of overlap, describing FA reductions in similar brain regions but with distinct degrees of specificity and generality (Fuzzy clustering (Bezdek, 1981)). These results suggest that the biclusters uncovered by GFM vary and are optimal in terms of their specificity and generality, as well as diversity, which is exemplified by the brain region described by them (see Methods).

**Topological organization of biclusters uncovers functionally meaningful local regions of FA reduction**

Because the identification of biclusters is not constrained by predefined knowledge about the anatomical region of the voxels, any grouping strategy may eventually identify sets of subjects sharing low FA values in voxels scattered throughout the whole brain. To evaluate the biological meaningfulness of FA reduction regions uncovered in the biclusters, our method topologically organized the eight biclusters into four main equivalence classes. The equivalence classes are defined by the partial order imposed by the non-dominance relationship among biclusters, that is, there is no better solution in both sensitivity and generality within each class (see Methods). Although “equivalent”, optimal biclusters within (and eventually across) these classes can be ordered on the basis of the inclusion of their subjects (Jech, 2003; Romero-Zaliz et al., 2008a; Zwir et al., 2005a,b) (see Methods, Table 1, and Supplementary Fig. 2). This organization of the classes is termed hierarchies, where biclusters located at the top and at the bottom of a hierarchy correspond to the most general and to the most specific observations. The obtained results cannot reject the null hypothesis of a different proportion of a particular gender than that of the original sample in each hierarchy (p-value > 0.1, after correction for multiple test, $B_{1,1}$ was omitted since it has only 5 members).

**Results**

Biclusters encode sets of voxels with FA reductions shared by subsets of subjects with SZ

We first investigated decreased FA regions in a sample composed of TBSS images from 47 SZ patients, which together did not exhibit significant differences from a similar sample composed of 36 images of healthy controls (see Statistical analysis, Methods, p-value > 0.81). A partition of the images corresponding to the patients with SZ using GFM–NMF uncovered eight optimal local partitions or biclusters, where each bicluster encoded a subset of subjects characterized by a similar degree of FA reduction in a particular subset of voxels. This method allowed any given subject and/or voxel to belong to more than one bicluster or to none of them (see Methods). The mean FA of the voxels in each of the eight biclusters significantly differed from the mean FA for voxels in the same location in either the other SZ subjects not included in that bicluster or from the healthy controls after correction for multiple comparisons (see Statistical analysis, Methods, Table 1, Figs. 3–4). This suggests that the biclusters should separately explain a large part of the variability in the population. In fact, 41 of the 47 SZ subjects were included in at least one bicluster (Table 1), which accounted for >95% of the FA variance across subjects (in the population) and suggests a high degree of generality. The biclusters varied in terms of their size, based on the associated numbers of subjects and shared voxels. For example, one general bicluster (i.e., one having high coverage) contained 21 subjects and 9744 voxels, while another specific bicluster (i.e., one having low coverage) contained only 5 subjects and 1322 voxels. While generality implies a large coverage of the sample; specificity displays smaller but more cohesively arranged and shared sets of FA voxels in the sample. The latter two biclusters did not overlap, and thus were associated with FA reductions in different brain regions, as expected. On the other hand, another pair of biclusters containing 15 subjects with 5147 voxels and 5 subjects with 2637 voxels respectively, showed a high degree of overlap, describing FA reductions in similar brain regions but with distinct degrees of specificity and generality (Fuzzy clustering (Bezdek, 1981)). These results suggest that the biclusters uncovered by GFM vary and are optimal in terms of their specificity and generality, as well as diversity, which is exemplified by the brain region described by them (see Methods).

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biclusters, respectively. Moreover, all biclusters in a hierarchy are optimal in the sense that one bicluster is not worse (i.e., dominated) than another in both the objectives of specificity and generality (i.e., see multiobjective/multimodal optimization (Deb, 2001a,b; Zwir et al., 2005a,b), Methods, Table 1). Disjoint hierarchies indicate diversity of biclusters, and thus provide a distributed coverage and description of the sample.

Re-mapping of FA reduction regions from biclusters onto the original TBSS images, revealed that voxels with decreased FA tended not to be scattered but to be confined to certain areas for each hierarchy, and were localized to white matter tracts potentially relevant to the pathophysiology of SZ (Fig. 5). The four identified hierarchies mapped to different anatomical regions (see Fig. 1 in Huang et al., 2011, Fig. 5).

The first hierarchy involved only one bicluster with decreased FA primarily in the genu of the corpus callosum (GCC) (Table 1, Fig. 5a). The second hierarchy included biclusters with patients involving FA reductions primarily in the fornix (FX) and/or in the external capsule (EC) (Table 1, Fig. 5b). The most general bicluster in this hierarchy included patients with FA reduction in both FX and EC, whereas another more specific bicluster in the same hierarchy differentiated a subset of patients with FA reduction only in the FX. The third hierarchy included biclusters with FA reductions in the retrolenticular limb of internal capsule (RLIC), and/or in the posterior limb of internal capsule (PLIC),...
and/or in the splenium of the corpus callosum (SCC) (Table 1, Fig. 5c).
Remarkably, the FA reduction in the SCC was not prominent in the most general bicluster of 21 subjects within this hierarchy; however, the FA reduction in the SCC was prominent in a more specific bicluster within the larger group of subjects. The fourth hierarchy partially overlapped with the third, and shared their most general bicluster (Supplementary Fig. 2). Despite this overlap, the most specific bicluster in the fourth hierarchy was different from the rest of the patients and the other biclusters (Table 1, Figs. 3–4), showing FA reductions in the anterior limb of internal capsule (ALIC, Fig. 5d).

Post hoc analysis of the subjects identified by disjoint biclusters uncovers distinct subsets of SZ patients with slightly different phenotypes.

To evaluate associations of each hierarchy’s FA reductions with clinical features, we analyzed scores of SAPS and SANS items and domains (Supplementary Table 1, Fig. 6). Subjects within the first hierarchy were more likely to have certain bizarre behavior symptoms (i.e., social–sexual behavior, aggressive behavior), certain formal thought disorder symptoms (i.e., derailment and pressured or distractible speech), and delusions of reference (Supplementary Table 1, Fig. 6). These symptoms were significantly associated with the bicluster exhibiting FA reduction in the GCC at

Fig. 5. Representation of low FA regions in white matter for different biclusters. Figures depict axial, sagittal, and coronal slice representations (left to right panels) of four biclusters mapping specific structural abnormalities (i.e., low FA), to regions on the brain white matter tracts. The utilized convention is that the right side corresponds to the right of the image. Gray pixels represent voxels included in the TBSS skeleton. Red pixels represent voxels from the TBSS skeleton that were identified by the corresponding biclusters (see Table 1). Biclusters are renamed as $B_{ij}$, where $i$ corresponds to a particular hierarchy, and $j$ to the order in such hierarchy (smallest $j$-value indicates the most general and top level bicluster). (a) Representation of Bicluster $B_{1,1}$. (b) Representation of Bicluster $B_{2,3}$. (c) Representation of Bicluster $B_{3,3}$. (d) Representation of Bicluster $B_{4,2}$.
Clinical relationships of biclusters. The bar plots show the averaged severity of positive (psychotic) symptoms (SAPS and SANS scales) for subjects included in bicluster $B_{1,1}$ (blue bars), bicluster $B_{2,3}$ (red bars), bicluster $B_{3,3}$ (green bars), bicluster $B_{4,2}$ (purple bars), and the rest of the patient sample (light blue bars). Biclusters are named as $B_{i,j}$, where $i$ corresponds to a particular hierarchy, and $j$ to the order in such hierarchy (smallest $j$-value indicates the most general and top level bicluster).

Significant differences in means of items exhibited by subjects of a particular bicluster are indicated with an asterisk (detailed statistics are indicated in Supplementary Table 1). Three sets of symptoms were linked with particular biclusters: delusion, bizarre behavior, and affective flattening or alogia symptoms were associated primarily with bicluster $B_{1,1}$ (blue brace), bicluster $B_{2,3}$ (red brace), and bicluster $B_{3,3}$ (green brace), respectively. SAPS and SANS items are grouped by their corresponding domains.
the item level (p-value < 5.00E − 02, Supplementary Table 1) and at the domain level (e.g., bizarre behavior, p-value < 1.88E − 02 after correction for multiple tests, Supplementary Table 2).

The second hierarchy was significantly associated (Supplementary Table 1, Fig. 6) with certain types of delusions (i.e., delusions of persecution, delusions of grandeur, delusions of control, mind reading delusions, thought insertion, and thought withdrawal). Although there was consistency across all clinical features in this hierarchy, specific biclusters showing FA reduction only in the FX were associated with more symptoms at the item level than general biclusters (p-value < 5.00E − 02, Supplementary Table 1) and at the domain level (e.g., delusions, p-value < 1.29E − 02 after correction for multiple tests, Supplementary Table 2). This was expected because fewer individuals tend to have more features in common than larger sets of individuals. Subjects in biclusters associated with the third hierarchy were more likely to have poverty of speech and callousness in their social and physical behavior (p-value < 5.00E − 02, Supplementary Table 1, Fig. 6). Finally, the fourth hierarchy did not have significant associations with any symptoms after Bonferroni corrections.

Discussion

Studies of white matter using diffusion weighted MRI in SZ have reported decreased FA in many regions, but increased FA in some tracts (see Table 1, Fig. 6). We recently characterized different types of SZ by describing its heterogeneous genotypic and phenotypic architecture (Arnedo et al., 2014), and confirmed such heterogeneity by uncovering distinct patterns of white matter anisotropy (Arnedo et al., 2015). Here, we further characterized different types of SZ by describing its heterogeneous genotypic and phenotypic architecture (Arnedo et al., 2014). Our method characterizes different types of SZ as characterized by abnormalities in different brain regions, just as we have shown elsewhere that different classes of schizophrenia can be distinguished by distinct patterns of genes and distinct sets of clinical features (Arnedo et al., 2014). Our studies suggest that uncovering voxel-based biclusters in SZ show promise in reducing heterogeneity that is usually concealed in groups of people with the diagnosis of SZ.

We used an unsupervised machine learning approach (Mitchell, 1997) here termed GM–NMF that decomposes a collection of images from different SZ patients into local partitions or biclusters (Madeira and Oliveira, 2004). This approach constructively combines the strength of different clustering algorithms (Supplementary Fig. 1) into a single method (Fig. 2) that exhibits flexibility and robustness in terms of critical parameters (e.g., number of clusters, degree of fuzziness) that often affect and, in turn, conceal the discovery of realistic patterns. Using our method, we identified several distinct patterns of FA reductions in SZ patients in a purely data-driven and unbiased manner. These patterns encoded as biclusters are optimal in terms of their specificity, sensitivity, and diversity. FA in brain regions of each bicluster was significantly different than those of the same regions in the rest of the subject sample and in the controls. Additionally, the derived biclusters remapped into 3rd order tensors represented as NIFTI 3D images, revealing that the biclusters were anatomically localized to white matter regions often associated with SZ (Lee et al., 2013; Liu et al., 2013; Skudlarski et al., 2013).

We identified low FA voxels in specific biclusters corresponding to discrete anatomical locations (i.e., GCC, SCC, FX, RILC, PLIC, EC, and ALIC), which have been previously implicated in the pathophysiology of SZ. Biclusters in the first and second hierarchies are consistent with published studies reporting lower FA values in the GCC and the FX have been reported in first-episode SZ patients (Lee et al., 2013). Abnormalities within the GCC reported in SZ are thought to affect inter-hemispheric communications (Sivagnanasundaram et al., 2007), whereas the FX is the major outflow pathway of the hippocampus (Fitzsimmons et al., 2009). The subjects in biclusters associated with decreased FA in the GCC were characterized primarily by disorganized symptoms. In contrast, subjects associated with FA reduction in FX were noted to have prominent delusions. Lastly, biclusters in the third hierarchy were associated with abnormalities in the SCC, and a relatively higher severity of negative symptoms. Correlations between biclusters and clinical features may be a direct consequence of a role of the specific white matter abnormalities in producing symptoms. This may suggest distinct underlying etiologies in different patients diagnosed with SZ. In other words, distinct classes of schizophrenia can be characterized by abnormalities in different brain regions, just as we have shown elsewhere that different classes of schizophrenia can be distinguished by distinct patterns of genes and distinct sets of clinical features (Arnedo et al., 2014). Our studies suggest that uncovering voxel-based biclusters in SZ show promise in reducing heterogeneity that is usually concealed in groups of people with the diagnosis of SZ.

Our method pursuing local partitions of brain images provides substantial advantages over classical clustering approaches. Averaging and comparing groups would be expected to miss real differences in FA if reductions are localized in different locations in each patient (Fig. 1). In contrast to classical clustering techniques, such as hierarchical clustering (Sokal and Michener, 1958) and k-means clustering (Hartigan and Wong, 1979), we used biclustering techniques that do not require patients in the same bicluster to perform similarly over all voxels exhibiting FA reduction. Classical clustering methods derive a global model whereas biclustering algorithms produce a local model in which signals emerge only in relevant dimensions.

Moreover, our approach does not require any assumption about the number of the patterns or biclusters. Establishing the optimal number of biclusters is an unsolved computational problem since different features emerge from different assumptions about this number (Bittner and Smith, 2003; Fraley and Raftery, 1998; Fred and Jain, 2005; Latore Carmona et al., 2013). Our method uncovers optimal biclusters defined in distinct granular partitions (e.g., multi-way/hierarchical tensor decomposition (Cichocki, 2009)) defined based on a distinct number of clusters without being exhaustive or redundant. Optimality was defined as a trade-off among specificity, generality, and diversity of the biclusters by multiobjective optimization.

We recently characterized different types of SZ by describing its heterogeneous genotypic and phenotypic architecture (Arnedo et al., 2014). Here, we confirmed such heterogeneity by uncovering distinct brain abnormalities associated with different phenotypes. The limitation of our approach is clearly dictated by the quality of the data, particularly in the phenotypic measurements. This problem is exacerbated in psychiatric disorders due to the clinical condition of the patients at the evaluation, the different scales and questionnaires utilized, and the fuzziness intrinsic to the symptoms being evaluated. These constraints often impede detection of significant relationships between brain abnormalities and phenotypic symptoms. In contrast, our results show that the uncovered biclusters are associated with different sets of clinical features of SZ as well as having statistically significant FA reductions in particular anatomical regions with functions relevant to the...
associated symptom patterns (Blanchard and Cohen, 2006; Holliday et al., 2009). Specifically the first group of subjects in the hierarchy displayed prominent bizarre behavior, the second group in the hierarchy displayed prominent delusions, and the third displayed prominent negative symptoms including disorganized speech (Supplementary Table 1, Fig. 6).

Together, our purely data-driven approach uncovered biclusters with statistically significant association between particular brain regions and distinct clinical features. The statistically significant and distinct clinical associations suggest that the biclusters are not a computational artifact. Therefore our results may provide clues about distinct pathophysiological processes that produce different forms of SZ. Our current method represents a novel approach to uncover latent patterns of whole-brain structural connectivity from DTI-derived TBSS data, and allows us to characterize complex relationships between different brain structures and functions with distinct sets of behavioral and cognitive features. This approach may be a pioneering contribution towards a foundation for precise person-centered diagnosis and treatment of psychotic disorders.

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**Arnedo et al., 2015**

**Acknowledgments**

This work was supported in part by the Spanish Ministry of Science and Technology TIN2009-13950, TIN2012-38805 including FEDER funds, the R.L. Kirschstein National Research Award to I.Z.; the National Institutes of Health including grant 5K08MH087720 to G.A.deE; K08MH085948 to D.M., and the National Institute of Mental Health MH066031 to D.M.B. G.A.deE is a Stepoken and Constance Lieber Investigator, and Sidney R. Baier Jr. Investigator, as well as Roksamp Chair of Biological Psychiatry at USF.

**Financial disclosures**

The authors report no financial relationships with commercial interest.

**Appendix A. Supplementary data**

Supplementary data to this article can be found online at http://dx.doi.org/10.1016/j.neuroimage.2015.06.083.

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